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Evaluation of Flooding due to Urbanization
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ABSTRACT

With urbanization, the watershed response to significant storm events changes due to the increase in imperviousness, the decrease in time of concentration, and possibly more importantly, the installation or lack of improvement to deficient flood control facilities. The effect on the environment is the significant alteration in the natural floodplain limits, which can aggravate other flooding situations due to the floodwaters crossing watershed boundaries. This cascading effect, where floodwaters which flood one watershed and then cross into another channel system, causing backwater and subsequent flooding, which in turn causes flooding into still another channel system. Such a scenario is common in large regions, which is composed of alluvial fan topography, characterized by gentle cross-slopes in one direction, but with a mild slope in the direction of the channel system. The capability to analyze this environmental problem escapes the capacity of most currently available computer models. That is, most hydrologic models involve routing components (e.g. kinematic wave, convex, etc.) which do not accommodate the important effects of backwater and subsequent escape of the flows from the channel without the user prescribing the flow path. In this paper, the Diffusion Hydrodynamic Model DHM23 is applied to a complicated flooding scenario in the county of Orange. The model represents the topography with a finite element discretization, and includes one-dimensional channel routing elements, constrictions, junctions, and an interface model to accommodate the escape (and return) of flood flows between channels and the topography. The DHM produces results which cannot be obtained by other currently available models, and the program can be run on the IBM compatible personal computers.

INTRODUCTION

Each year, flood control projects and storm channel systems are constructed by Federal, State, County and City governmental agencies and also by private land developers which accumulatively cost in the billions of dollars. Additionally, floodplain insurance mapping, zoning, and insurance rates are continually being prepared or modified by the Federal Emergency Management
Agency. Finally, the current state-of-the-art in flood system
deficiency analysis often results in the costly reconstruction
of existing flood control or protection measures which are based
upon widely used analysis techniques which often are not adequate
to represent the true hydraulic/hydrologic response of the flood
control system to the standardized design storm protection level.
The main drawbacks in the currently available analysis techniques
lie in the inability of the current models to represent unsteady
backwater effects in channels and overland flow, unsteady over-
flow of channel systems due to constrictions (e.g., culverts,
bridges, etc.), unsteady flow of floodwater across watershed
boundaries due to two-dimensional (horizontal plane) backwater,
and ponding flow effects.

In this paper, we report on the current state of development of
a Diffusion Hydrodynamic Model (DHM) which approximates all of
the above hydraulic effects for channels, overland surfaces, and
the interfacing of these two hydraulic systems to represent channel
overflow and return flow. The overland flow effects are modeled
by a two-dimensional unsteady flow hydraulic model based on the
diffusion form of the governing flow equations. Similarly, channel
flow is modeled using a one-dimensional unsteady flow hydraulic
model based on the diffusion equation. The resulting models both
approximate unsteady supercritical and subcritical flow (without
the user predetermining hydraulic controls), backwater flooding
effects, and escaping and returning flow from the two-dimensional
overland flow model to the channel system.

The current simple version of the DHM has been successfully applied
to a collection of one-and two-dimensional unsteady flows hy-
draulic problems including dam-break analyses and flood system
deficiency studies. Consequently, the proposed DHM promises to
result in a highly useful, accurate, and simple to use computer
model which is of immediate help to practicing flood control
engineers (however, considerable topographic data may be needed
depending on the area being modeled).

Background
One approach to studying flood wave propagation is to simply
estimate a maximum possible flow rate and route this flow as a
steady state flow through the downstream reaches. This method
is excessively conservative in that all effects due to the time
variations in channel storage and routing are neglected.

A better approach is to rely on one-dimensional (1-D) full
dynamic unsteady flow equations (e.g., St. Venant eqs.). Some
sophisticated 1-D models include more terms and parameter to
account for complexities in prototype reaches which the basic
flow equations cannot adequately handle. However, the ultimate
limit of the 1-D model can only be overcome by extending into
the two-dimensional (2-D) realm. Several 2-D models employing
full dynamic equations have been developed. Among them is one
particularly aimed at flood flow analysis by Katopodes and
Strelkoff7. Attendant with the increased power and capacity of
2-D fully dynamic models, are the greatly increased boundary, initial, geometry and other input data requirements they need for large amounts of computer memory and computational speed, as well as the increased computational time. Although it is often claimed that the extra computational cost and effort required for a more sophisticated model is negligible compared with the total modeling cost and effort in the 1-D realm, the parallel in the 2-D realm seems to be premature at present.

A coupled 1-D and 2-D diffusion hydrodynamic model (DHM) described in this paper appears to offer a simple and economic means for the estimation of flooding effects for diverging flood flows.

**ONE-DIMENSIONAL MODEL FOR UNSTEADY FLOW**

Generally, the 1-D flow approach is used wherever there is no significant lateral variation in the flow. Land,

8,9 examines four such unsteady flow models in their prediction of flooding levels and flood wave travel time, and compares the results against observed unsteady flow data. Ponce and Tsivoglou,

10 examine the gradual failure of an earth embankment (caused by an overtopping flooding event) and present a detailed model of the total system: sediment transport, unsteady channel hydraulics, and earth embankment failure. Although many dam-break studies involve flood flow regimes which are truly two-dimensional (in the horizontal plane), the 2-D case has not received much attention in the literature. In addition to the aforementioned model of Katopodes and Trelhoff, which relies on the complete 2-D dynamic equations, Xanthopoulos and Koutitas,

11 use the diffusion model to approximate a 2-D flow field. The model assumes that the flood plain flow regime is such that the inertia terms are negligible. In a 1-D model, Akan and Yen,

1 also use the diffusion approach to model hydrograph confluences at channel junctions. In the latter study, comparisons of model results were made between the diffusion model, a complete dynamic wave model solving the total equation system, and the basic kinematic wave equation model. The comparisons between the diffusion model and the dynamic wave model were good for the study cases, showing only minor discrepancies.

**MODEL ACCURACY IN PREDICTION OF FLOOD DEPTHS**

In order to evaluate the accuracy of the proposed diffusion model in the prediction of flood depths, Land's model,

8,9, referred to in the preceding section, was used for comparison purposes. This model solves 1-D full dynamic equations by an implicit finite scheme and is identified as the USGS dynamic model K634. The study approach was to compare predicted flood depths for various channel slopes and inflow hydrographs using the above two models.
From the study of Hromadka, et al.\textsuperscript{2} it is seen that the diffusion model provides estimates of flood depths that compare very well to the flood depths predicted from the K-634 model. Differences in predicted flood depths are less than three percent for the various channel slopes and peak flow rates considered.

In the following sections, the development of a two-dimensional diffusion hydrodynamic model (DHM) will be described. The model is based on a diffusion scheme in which the gravity, friction, and pressure forces are assumed to dominate the flow equations. Earlier, Xanthopoulos and Koutitas\textsuperscript{11} employed such an approach in the prediction of dam-break flood plains in Greece. Good results were also obtained in their studies applying the 2-D model to flows that are essentially 1-D in nature. In the following, an integrated finite difference model is developed which (1) solves the two-dimensional topographic flood wave propagation, (2) the one-dimensional flood wave propagation for channel flow, and (3) the interface between the two models to accommodate flooding effects.

**MATHEMATICAL DEVELOPMENT FOR TWO-DIMENSIONAL MODEL**

The set of (fully dynamic) 2-D unsteady flow equations consist of one equation of continuity

\[
\frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} + \frac{\partial H}{\partial t} = 0
\]  

(1)

and two equations of motion

\[
\frac{\partial q_x}{\partial t} + \frac{\partial}{\partial x} \left[ \frac{q_x^2}{h} \right] + \frac{\partial}{\partial y} \left[ \frac{q_x q_y}{h} \right] + gh \left[ S_{fx} + \frac{\partial H}{\partial x} \right] = 0
\]  

(2)

\[
\frac{\partial q_y}{\partial t} + \frac{\partial}{\partial x} \left[ \frac{q_y^2}{h} \right] + \frac{\partial}{\partial y} \left[ \frac{q_x q_y}{h} \right] + gh \left[ S_{fy} + \frac{\partial H}{\partial y} \right] = 0
\]  

(3)

in which \(q_x, q_y\) are flow rates per unit width in the x,y-directions; \(S_{fx}, S_{fy}\) represent friction slopes in x,y-directions; \(H, h, g\) stand for, respectively, water-surface elevation, flow depth, and gravitational acceleration; and \(x, y, t\) are spatial and temporal coordinates.

The above equation set is based on the assumptions of constant fluid density with zero sources or sinks in the flow field, hydrostatic pressure distributions, and relatively uniform bottom slopes.
The local and convective acceleration terms can be grouped together such that they are rewritten as

\[ m_z + \left[ S_{fz} + \frac{\partial H}{\partial z} \right] = 0, \ z = x, y \]  

(4)

where \( m_z \) represents the sum of the first three terms in Eqs. (2) and (3) divided by \( gh \). Assuming the friction slope to be approximated by steady flow conditions, the Manning's formula in the U.S. customary units can be used to estimate \( q_z \)

\[ q_z = \frac{1.486}{n} h^{5/3} S_{fz}^{1/2}, \ z = x, y \]  

(5)

Equation 5 can be rewritten as

\[ q_z = -K_z \frac{\partial H}{\partial z} - K_z m_z, \ z = x, y \]  

(6)

where

\[ K_z = \frac{1.486}{n} h^{5/3} \left| \frac{\partial H}{\partial s} + m_s \right|^{1/2}, \ z = x, y \]  

(7)

The symbol \( s \) indicates the flow direction which makes an angle \( \theta = \tan^{-1} (q_y/q_x) \) with the \( x \)-direction.

Values of \( m \) are assumed negligible by several investigators\(^1\)\(^,\)\(^2\)\(^,\)\(^7\), resulting in the simple diffusion model:

\[ q_z = -K_z \frac{\partial H}{\partial z}, \ z = x, y \]  

(8)

The proposed 2-D flood flow model is formulated by substituting Equation 8 into Equation 1,

\[ \frac{\partial}{\partial x} K_x \frac{\partial H}{\partial x} + \frac{\partial}{\partial y} K_y \frac{\partial H}{\partial y} = \frac{\partial H}{\partial t} \]  

(9)

**NUMERICAL MODEL FORMULATION (GRID ELEMENTS)**

For uniform grid elements, the numerical modeling approach used is the integrated finite difference version of the nodal domain integration (NDI) method. For grid elements, the NDI nodal equation is based on the usual nodal system (see Fig. 3). Flow rates along the boundary \( \Gamma \) are estimated using a linear trial function assumption between nodal points.
For a square grid of width $\delta$,

$$q_{\Gamma_E} = -K_{x_{\Gamma_E}} \left\{ \frac{K_{x_{\Gamma_E}}}{\delta \cos \theta} \right\} \left( H_E - H_C \right) / \delta$$

(10)

where

$$K_{x_{\Gamma_E}} = \left\{ \frac{1.486}{n} \right\} \delta \cos \theta \frac{1/2}{\left| H_E - H_C \right|}$$

(11)

$$0 ; \bar{h} \leq 0 \text{ or } \left| H_E - H_C \right| < 10^{-3}$$

In Equation 11, $h$ and $n$ are both the average of the values at $c$ and $E$, i.e. $h = (h_C + h_E)/2$ and $n = (n_C + n_E)/2$. Additionally, the denominator of $K_{x_{\Gamma_E}}$ is checked such that $K_{x_{\Gamma_E}}$ is set to zero if $\left| H_E - H_C \right|$ is less than a tolerance such as $10^{-3}$ ft.

The model advances in time by an explicit approach

$$H_{i+1} = K_i H_i$$

(12)

where the assumed input flood flows are added to the specified input nodes at each time step. After each time step, the conduction parameters of Eq. (11) are reevaluated, and the solution of Eq. (12) reinitiated. Using grid sizes with uniform lengths of one-half mile, time steps of size 3.6 sec were found satisfactory. Verification of the 2-D model is given in Hromadka², Hromadka et al.², Hromadka and Durbin³m abd Hromadka and Lai⁴. Hromadka and DeVries⁵ demonstrate the use of the two-dimensional model in the analysis of dam-break flood plains.

MATHMATICAL DEVELOPMENT FOR ONE-DIMENSIONAL MODEL

By eliminating a directional component in Eq. (9), a one-dimensional formulation is developed which provides a good approximation of one-dimensional unsteady flow routing including backwater effects and subcritical/supercritical flow regimes. Hromadka⁵ demonstrates the good results obtained from a one-dimensional version of DHM to model unsteady flow effects. Figure 1 shows the comparison between 1-D DHM results and the USGS K-634 model results for various channel slopes, and peak flow rates. The figure illustrates that good results are obtained from the DHM.
Figure 1. Diffusion model ( ○ ), kinematic routing (dashed line) and K-634 model results (solid line) for 1,000-foot width channel, Manning's $n = 0.040$, for various channel slopes, $S_0$. 

DAM-BREAK HYDROGRAPH

FLOW RATE (CFS)

TIME (HRS.)

(PEAK Q = 400,000 CFS)

(PEAK Q = 120,000 CFS)

MAXIMUM WATER DEPTH (FT.)

DISTANCE FROM DAM-BREAK (MILES)
INTERFACE MODEL (FLOODING SOURCE/SINK TERM)

To model flood flows exiting from and returning to a one-dimensional channel, an interface model is needed to couple the 1-D DHM and 2-D (topography) DHM. Figure 2 illustrates the mass conservation scheme assumed to represent the source/sink term of flows flooding/draining from the topographic model to the channel model.

Figure 2. DHM interface model
INCLUSION OF CHANNEL DEFICIENCY EFFECTS

The main cause of existing flood plain difficulties is the existence of channel constrictions due to bridges, undersized culverts, and other factors. By specifying a stage-discharge relationship at points within the channel system (or on the topography), constrictions are modeled efficiently in the DHM.

Preliminary Results

Herein we will describe our most current and advanced work. The 1-D and 2-D DHM formulations are coupled through the interface model of the flooding source/sink term (due to channel overflows onto the topographic model). Using simple grid elements, Figure 3 shows the integrated finite difference scheme for the mass balance. Figure 4 shows the problem definition involving 160 grid elements for the topographic model and 3 channel systems. Included in the middle channel system is a junction. The channel systems drain towards culverts (located at the bottom of the domain) which have a limited capacity (e.g., freeway crossings). Figure 5 shows the channel inflow hydrographs and pertinent topographic data to indicate catchment divides. Figures 6, 7, 8, 9, and 10 show the flood plain extent at various model time values. Figure 11 shows the three channel outflow hydrographs which reflect the release of ponded waters due to culvert deficiencies. Figure 12 shows the hydrographs at grid points 1 and 2 as flow escapes to the left of the domain. (For this application, zero flux is assumed on the right side of the domain, with critical depth assumed for the left side). Figures 13 and 14 show the maximum flood depths calculated in both plan and profile views, respectively.

An examination of the model results indicate that the current simple version of the DHM already provides a considerable advance in floodplain determination over that currently available.

CONCLUSIONS

The DHM provides a novel tool for hydrologic and hydraulic engineers who are involved in floodplain management or flood control. By the continuing development of this new modeling approach, the analysis of flood control system deficiencies and development of methodology on how to best spend the available dollars is now feasible in both a qualitative and quantitative sense.
Figure 3. Grid element nodal molecule

Figure 4. DHM model discretization of a hypothetical watershed
Figure 5. Inflow and outflow boundary conditions for the hypothetical watershed model

Figure 6. DHM modeled floodplain at time = 1-hour
Figure 7. DHM modeled floodplain at time = 2-hours

Figure 8. DHM modeled floodplain at time = 3-hours
Figure 9. DHM modeling floodplain at time = 5-hours

Figure 10. DHM modeled floodplain at time = 7-hours
Figure 11. Outflow hydrograph at nodes 31, 71 and 121 (assumed outflow relation: $Q = 10d$)
Figure 12. Critical outflow hydrograph at nodes 1 and 2

Figure 13. Maximum water depth at different cross-sections
Figure 14. Maximum water profiles
REFERENCES


