

A simple hydrologic mass balance model

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A simple hydrologic mass balance model has been developed to study the time evolution of soil-water storage in an urban watershed. Advantages of using the mass balance model is that it only requires climatological data, it is easy to implement, and the model provides a synthetic record of long-term watershed behaviour. Water conservation can be analysed by varying the model parameters, such as infiltration rate, irrigation water, among other factors.

INTRODUCTION

Numerous mathematical models have been developed to simulate various hydrologic systems. An extensive literature review by Hromadka (1986) indicates that the simpler hydrologic models perform as good as or better than the more complex hydrologic models. In this paper, the focus is not upon runoff rates developed from storm events, but rather upon the time evolution of soil-water storage to the effects of rainfall, irrigation, evapotranspiration, and other factors. A simple hydrologic mass balance model is developed which accommodates several important mass-balance elements, using data which is readily obtained by field inspection or from local agency resources.

The hydrologic soil-water mass (water) balance model can be represented by the following mass balance equation:

$$I - O = \frac{\Delta s}{\Delta t} \quad (1)$$

where

I = inflow per unit time

O = outflow per unit time

$\Delta s/\Delta t$ = the change in storage within the system per unit time

The uncertainties of the mass balance equation (equation (1)) lie mainly in the inability to properly measure or estimate the various inflow (I) and outflow (O) terms. Nevertheless, the mass balance model is a useful tool to simulate a long-term hydrologic system, such as the soil-water storage in a typical residential subdivision lot.

MODEL DESCRIPTIONS

A more generalized version of the mass balance equation will explain the various components of the hydrologic

cycle and provide an insight to the problem-solving techniques. The hydrologic budget can be represented as

$$P + I_r - ET - I_t - I_f - S_d - R = \Delta s \quad (2)$$

where

P = precipitation per unit time

I_r = irrigation per unit time

ET = evapotranspiration per unit time

I_t = vegetation interception per unit time

I_f = infiltration per unit time

S_d = surface detention per unit time

R = surface runoff per unit time

Δs = change in storage per unit time

Precipitation submodel

In this submodel, the continuous rainfall record is used. If raingage data are unavailable within the study area, then nearby rainfall station records should be used with geographical adjustment.

Irrigation submodel

In the urban watershed, the irrigation water is limited to lawn and garden usages. By subtracting the averaged water usage per capita, per household, from the water meter record, the averaged irrigation water can be estimated for each household.

Evapotranspiration submodel

An equation for estimating evapotranspiration developed by the Agricultural Research Service (ARS) is used in this submodel. The evapotranspiration for any given day is determined as follows (Holtan *et al.*, 1975):

$$ET = GI \cdot k \cdot E_p \cdot \left(\frac{S - SA}{AWC} \right)^x \quad (3)$$

where

ET = evapotranspiration (in/day)

GI = growth index of crop in % of maturity

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Table 1. Hydrologic capacities of soil texture classes

Texture class	S (%)	G (%)	AWC (%)	x AWC/G
Coarse sand	24.4	17.7	6.7	0.38
Coarse sandy loam	24.5	15.8	8.7	0.55
Sand	32.3	19.0	13.3	0.70
Loamy sand	37.0	26.9	10.1	0.38
Loamy fine sand	32.6	27.2	5.4	0.20
Sandy loam	30.9	18.6	12.3	0.66
Fine sandy loam	36.6	23.5	13.1	0.56
Very fine sandy loam	32.7	21.0	11.7	0.56
Loam	30.0	14.4	15.6	1.08
Silt loam	31.3	11.4	19.9	1.74
Sandy clay loam	25.3	13.4	11.9	0.89
Clay loam	25.7	13.0	12.7	0.98
Silty clay loam	25.3	8.4	14.9	1.77
Sandy clay	19.4	11.6	7.8	0.67
Silty clay	21.4	9.1	12.3	1.34
Clay	18.8	7.3	11.5	1.58

S = total porosity - 15 bar moisture %, G = total porosity - 0.3 bar moisture %, and AWC = S minus G

k = ratio of GI to pan evaporation, usually 1.0-1.2 for short grasses, 1.2-1.6 for crops up to shoulder height, and 1.6-2.0 for forest

E_p = pan evaporation (in./day)

S = total porosity of soil

SA = available porosity (unfilled by water)

X = AWC/G (G = moisture freely drained by gravity)

Equation (3) is used by the ARS in its USDAHL-74 model of watershed hydrology in combination with GI curves to calculate daily evapotranspiration. Representative values for S , G , and AWG are given in Table 1.

Vegetation interception submodel

The amount of water intercepted is a function of (1) the storm character, (2) amount of plant foliage and its character and orientation, and (3) the season of the year. For long-term hydrologic simulation, a constant interception storage that will be retained on the foliage against the forces of wind and gravity (usually varies between 0.01 and 0.05, Viessman *et al.*, 1977) is used in this submodel.

Infiltration submodel

The rate of infiltration is influenced by the type and extent of vegetal cover, the condition of the surface crust, temperature, rainfall intensity, physical properties of the soil, and water quality. The volume of storage available below ground is also a factor affecting infiltration rates. The ϕ -index model (Viessman *et al.*, 1977) is used in this submodel.

Surface detention submodel

Precipitation that reaches the ground may infiltrate, flow over the surface, or become trapped in numerous small depressions from which the only escape is evaporation or infiltration. In this model, the surface detention storage can be either increased to its maximum capacity by rainfall or decreased to zero by evaporation and/or infiltration.

Surface runoff submodel

In this model, the surface runoff is defined as the sum of excess precipitation and irrigation water. No flow routing is used in this submodel.

Storage submodel

Subsurface storage and groundwater storage are included in this submodel. The rules for interaction between subsurface storage and groundwater storage are as follows:

1. the subsurface storage has to be filled first,
2. after subsurface storage reaches a prescribed level, the water deep-percolates into the groundwater storage,
3. a portion of the groundwater storage is available for consumptive use through capillary soil-water flow when the subsurface storage is totally depleted, and
4. no subsurface water movement is included in this model.

MODEL USAGES

In general, the hydrologic mass balance (budget) model is a useful tool for simulating the long term soil-water storage evolution. A primary usage of this model is for analysis of water conservation. By investigating each submodel, different strategies can be studied to achieve a water conservation goal. Therefore, a thorough study of the entire hydrologic system should be conducted before the final planning is made. Finally, the economic, political, and aesthetic aspects should be incorporated in making the final planning.

DATA REQUIREMENTS

Hydrologic data are needed to describe precipitation, evaporation, transpiration, infiltration, and other components of the hydrologic system. Sources of data are numerous, with the US Geological Survey being a major source for streamflow and groundwater data. The National Weather Service (NOAA or National Oceanic and Atmospheric Administration) is the major collector of meteorologic data. Many other federal, state, and local agencies and other organizations also compile hydrologic data.

Precipitation data

Daily rainfall data and continuous rainfall data are best suited for the long term and short term hydrologic system simulation, respectively.

Irrigation data

In agricultural areas, water meter records can be used to determine the irrigation water consumption. In urban watersheds, the irrigation water consumption has to be interpolated for each household from its water meter record.

Pan evaporation and temperature data

Pan evaporation data is often scarce to obtain. Therefore, the temperature data can be used to correlate the available pan evaporation data to the study site.

Vegetation interception data

An area-averaged interception storage should be estimated for the study area by calculating the weighted average of different plant types and their foliage coverages.

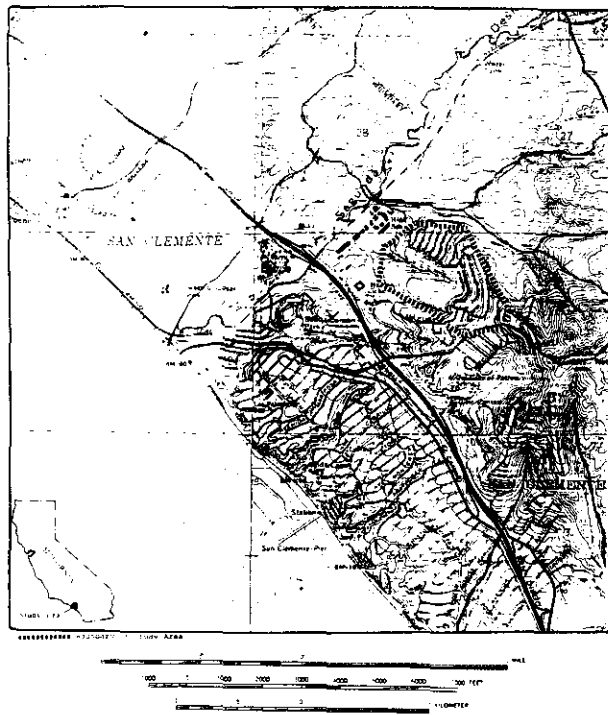


Fig. 1. Location map for study area

Infiltration data

For long-term hydrologic system simulation, an area-averaged infiltration rate can be estimated from the S.C.S. hydrologic soil groups (US Bureau of Reclamation, 1973).

Surface detention data

Surface data can be obtained from field investigation.

Surface runoff and groundwater storage data

Either surface runoff data or groundwater data is need to calibrate the hydrologic mass balance model.

APPLICATION

A simple hydrologic mass balance model is developed for a small residential area in an urban watershed at the City of San Clemente, California (Fig. 1). All the surface waters are drained into the streets, and then carried into a storm drain system. The main concern is the slope stability of this hillside residential community. The instability of the slope is suspected to be due to the changing of the subsurface and groundwater storages after watershed urbanization.

Daily precipitation data are obtained from the OCEMA (Orange County Environmental Management Agency). Daily temperature data are obtained from the California Climatological Data. Monthly pan evaporation data are also obtained from OCEMA at the nearby station which is correlated to the daily temperature data to approximate the daily evapotranspiration value. No stream gage nor groundwater data are available. New groundwater observation wells have been installed in this area to record the change of subsurface and groundwater storages. When this information is available, the hydrologic mass balance model can be calibrated. An example model output is included hereafter to depict the model schematic and assumptions, and also illustrates the results of the computer code supplied in Appendix B.

REFERENCES

- 1 Holtan, H. N., Stilte, G. J., Henson, W. H. and Lopez, N. C. USDAHL-74 Revised Model of Watershed Hydrology, US Department of Agriculture, ARS Tech. Bulletin No. 1518, Washington DC, 1975
- 2 Hromadka II, T. V. The State-of-the-art in Hydrologic Models: A Review of Progress. Proceedings: ENVIROSOFT '86 Conference, Newport Beach, California. Computational Mechanics Publications, 1986
- 3 US Bureau of Reclamation, Design of Small Dams, P.544. US Government Printing Office, Washington DC, 1973
- 4 Viessman, W., Jr, Knapp, J. W., Lewis, G. L. and Harbaugh, T. E. Introduction to Hydrology, 2nd ed., IEP Publishers, New York, 1977

APPENDIX A

INPUT SEQUENCES AND OUTPUT RESULTS

SURFACE-SUBSURFACE WATER BUDGET MODEL

```

ENTER A [1] TO CREAT A NEW DATA FILE
      OR A [2] TO EXECUTE AN EXISTING FILE
      OR A [3] TO EXIST PROGRAM
=====> 1
ENTER THE FILE NAME THAT STORES THE INPUT DATA
=====> T1.DAT
ENTER TOTAL AREA (SQUARE FEET) = 5000
ENTER MAXIMUM SUBSURFACE STORAGE (CUBIC FEET) = 25000
ENTER INITIAL SUBSURFACE STORAGE (CUBIC FEET)
ALLOWABLE VALUE IS BETWEEN [0] AND [ 25000.00]
=====> 0
ENTER DRIVE WAY AND ROOF COVERAGE (%)
ALLOWABLE VALUE IS BETWEEN [0] AND [100]
=====> 45
ENTER TREE AND BUSH COVERAGE (%)
ALLOWABLE VALUE IS BETWEEN [0] AND [55.0]
    
```

```

=====> 5
ENTER DEPTH (INCHES) OF INTERCEPTION
=====> .1
ENTER CONCRETE WALK WAY AND PATIO COVERAGE (%)
ALLOWABLE VALUE IS BETWEEN [0] AND [50.0]
=====> 5

ENTER GRASS COVERAGE (%)
ALLOWABLE VALUE IS BETWEEN [0] AND [45.0]
=====> 25
IMPERVIOUS PONDING AREA
ENTER PONDING AREA(%) THAT DRAINS TO IMPERVIOUS AREA
ALLOWABLE VALUE IS BETWEEN [0] AND [20.0]
=====> 5
ENTER PONDING DEPTH (INCHES)
=====> 1
ENTER PONDING AREA(%) THAT DRAINS TO PERVIOUS AREA
ALLOWABLE VALUE IS BETWEEN [0] AND [15.0]
=====> 0
PERVIOUS PONDING AREA
ENTER PONDING AREA(%) THAT DRAINS TO IMPERVIOUS AREA
ALLOWABLE VALUE IS BETWEEN [0] AND [15.0]
=====> 5
ENTER PONDING DEPTH (INCHES)
=====> 1
ENTER PONDING AREA(%) THAT DRAINS TO PERVIOUS AREA
ALLOWABLE VALUE IS BETWEEN [0] AND [10.0]
=====> 0
ENTER AREA (%) SLOPE AWAY FROM HOUSE
ALLOWABLE VALUE IS BETWEEN [0] AND [10.0]
=====> 5
PERCENT OF BARE LAND AREA IS 5.0 %

```

T1.DAT ...DATA FILE HAS BEEN CREATED

```

SURFACE-SUBSURFACE WATER BUDGET MODEL
ENTER A [1] TO CREAT A NEW DATA FILE
      OR A [2] TO EXECUTE AN EXISTING FILE
      OR A [3] TO EXIST PROGRAM
=====> 2
ENTER THE FILE NAME THAT STORES THE INPUT DATA
=====> T1.DAT
ENTER THE FILE NAME THAT STORES THE OUTPUT RESULTS
=====> TEST.OUT
INFILTRATION MODEL IS APPROXIMATED BY
      A CONSTANT SOIL LOSS RATE

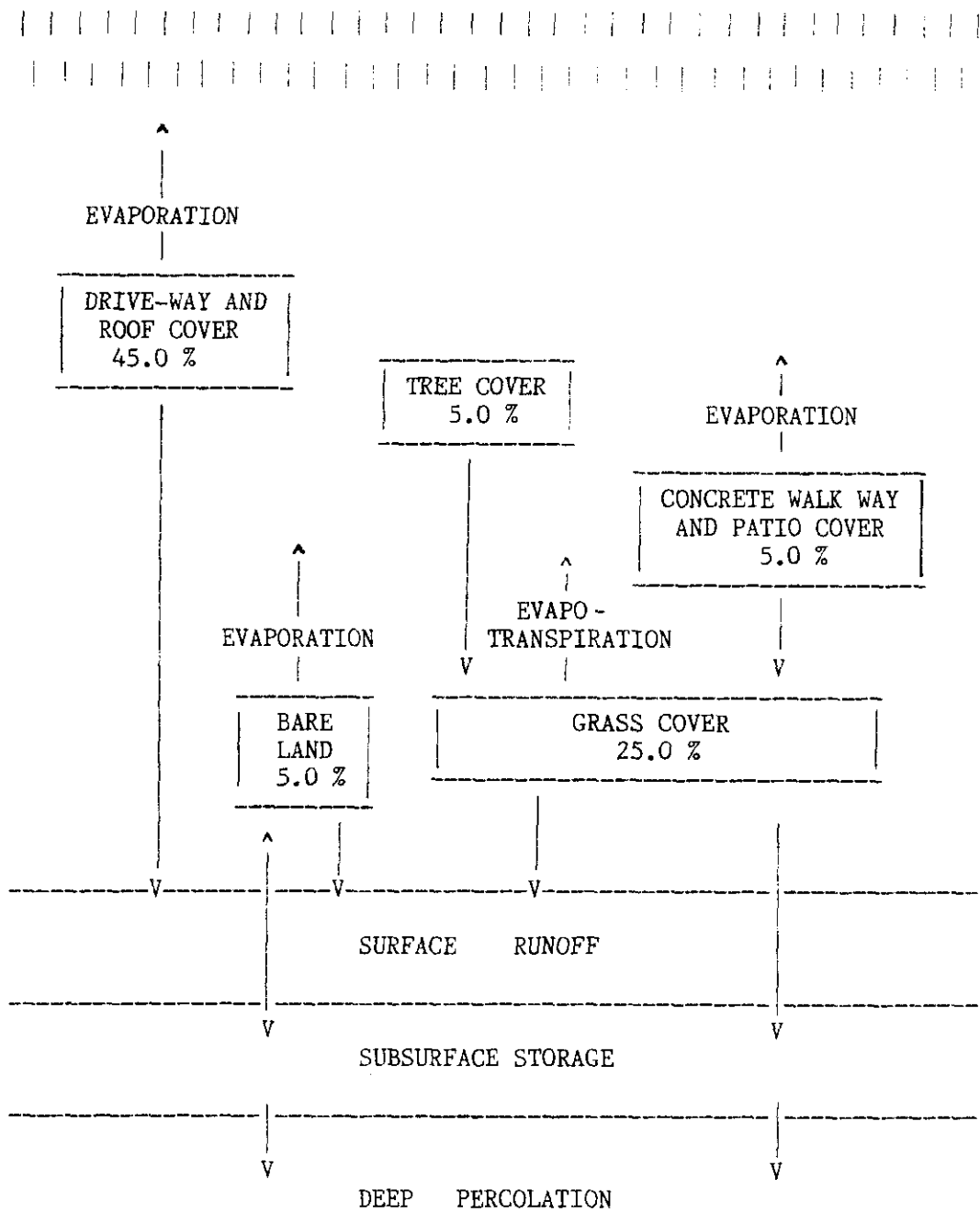
ENTER CONSTANT SOIL LOSS RATE (IN/HR) = .2
ENTER PERCENT (%) OF GROUNDWATER STORAGE THAT
CAN BE USED BY E.T. AFTER SUBSURAFCE STORAGE WAS
DEPLETED BY E.T.
=====> 30
ENTER LONG TERM AVERAGE IRRIGATION WATER DEPHT (IN)
=====> .5
DO YOU WANT TO OUTPUT A DAILY WATER BUDGET FOR
A USER SPECIFIED MONTH AND YEAR (Y/N) =====> N

```

==> END OF WATER BUDGET SIMULATION <==

NOTE: YOUR OUTPUT IS STORED IN [TEST.OUT]

RAINFALL



.....

PERCENT OF IMPERVIOUS PONDING AREA THAT DRAINS TO IMPERVIOUS AREA = 5.0(%)
 PERCENT OF IMPERVIOUS PONDING AREA THAT DRAINS TO PERVIOUS AREA = .0(%)
 PERCENT OF PERVIOUS PONDING AREA THAT DRAINS TO IMPERVIOUS AREA = 5.0(%)
 PERCENT OF PERVIOUS PONDING AREA THAT DRAINS TO PERVIOUS AREA = .0(%)
 PERCENT OF AREA THAT SLOPES AWAY FROM THE HOUSE = 5.0(%)

=====

NOTE : TOTAL AREA = 5000.00 SQUARE FEET
 MAXIMUM SUBSURFACE STORAGE = 25000.00 CUBIC FEET
 INITIAL SUBSURFACE STORAGE = .00 CUBIC FEET

=====

MODEL ASSUMPTIONS

=====

1. This model is based on the Water Budget Method, i.e.,
RAINFALL - E.T. - INFILTRATION = CHANGE OF STORAGE
2. Rainfall is in inches/day.
3. E.T. is the sum of evaporation from pervious and impervious areas and transpiration from plants.
4. Infiltration includes infiltration into subsurface storage and deep percolation into groundwater storage.
5. Infiltration rate is approximated by
the constant soil loss rate = 0.200 (in/hr).
6. The deep percolation occurs when the subsurface storage is greater than the maximum subsurface storage. The deep percolation volume is then set equal to volume which exceeds the maximum subsurface storage.
7. Storage includes subsurface and groundwater storages.
8. Subsurface storage is available for E.T. and part of the groundwater storage is available for E.T.
9. It is assumed that 30 percent of the groundwater storage is available for E.T. when subsurface storage is depleted.
10. It is assumed that the long term irrigation water which applies to the ponding and grass areas is equal to 0.5 inches/day.
11. It is assumed that the depth of interception for tree and bush is 0.1 inches.
12. Ponding depth of impervious area that drains to impervious area is 1.0 inches.
13. Ponding depth of impervious area that drains to pervious area is 0.0 inches.
14. Ponding depth of pervious area that drains to impervious area is 1.0 inches.
15. Ponding depth of pervious area that drains to pervious area is 0.0 inches.

1962 WATER BUDGET SUMMARY

	RAINFALL VOLUME (CU.FT.)	E.T. VOLUME (CU.FT.)	SURFACE/SUBSURFACE STORAGE (CU.FT.)	DEEP PERCOLATION (CU.FT.)	SURFACE RUNOFF (CU.FT.)	AVERAGED TEMPERATURE (°F)
JAN	NO RAINFALL DATA					
FEB	NO RAINFALL DATA					
MAR	NO RAINFALL DATA					
APR	NO RAINFALL DATA					
MAY	NO RAINFALL DATA					
JUN	NO RAINFALL DATA					
JUL	NO RAINFALL DATA					
AUG	NO RAINFALL DATA					
SEP	.00	464.86	20.83/ 1535.77	.00	166.04	73.0 °F
OCT	4.17	476.93	20.83/ 3093.00	.00	230.42	70.3 °F
NOV	29.17	488.71	20.83/ 4579.71	.00	241.25	67.0 °F
DEC	8.33	421.65	20.83/ 6156.18	.00	270.62	64.1 °F
SUM	41.67	1852.15	20.83/ 6156.18	.00	908.33	
AVG.						

1963 WATER BUDGET SUMMARY

	RAINFALL VOLUME (CU.FT.)	E.T. VOLUME (CU.FT.)	SURFACE/SUBSURFACE STORAGE (CU.FT.)	DEEP PERCOLATION (CU.FT.)	SURFACE RUNOFF (CU.FT.)	AVERAGED TEMPERATURE (°F)
JAN	83.33	550.92	22.92/ 7659.39	.00	287.55	62.6 °F
FEB	1195.83	1341.78	20.83/ 8863.60	.00	693.58	67.8 °F
MAR	879.17	2576.36	20.83/ 9050.79	.00	376.04	65.5 °F
APR	387.50	3048.83	1.01/ 8526.87	.00	69.92	65.0 °F
MAY	25.00	3279.03	.00/ 7534.27	.00	.00	68.0 °F
JUN	8.33	2633.69	2.13/ 7094.28	.00	.00	69.8 °F
JUL	.00	1679.49	20.83/ 7541.15	.00	115.35	72.9 °F
AUG	.00	1546.47	20.83/ 8107.20	.00	147.89	76.1 °F
SEP	1208.33	1603.54	20.83/ 9252.53	.00	646.96	81.8 °F
OCT	145.83	1226.39	20.83/10198.45	.00	233.92	74.7 °F
NOV	2291.67	1166.77	20.83/12212.60	.00	1298.25	69.0 °F
DEC	.00	878.54	20.83/13374.79	.00	219.69	68.2 °F
SUM	6225.00	21531.81	20.83/13374.79	.00	4089.15	
AVG.	518.75	1794.32		.00	340.76	70.1 °F

⋮

1984 WATER BUDGET SUMMARY

	RAINFALL VOLUME (CU.FT.)	E.T. VOLUME (CU.FT.)	SURFACE/SUBSURFACE STORAGE (CU.FT.)	DEEP PERCOLATION (CU.FT.)	SURFACE RUNOFF (CU.FT.)	AVERAGED TEMPERATURE (°F)
JAN	104.17	1160.81	20.83/16765.26	.00	225.14	70.3 °F
FEB	62.50	2929.75	.00/16033.42	.00	.00	69.8 °F
MAR	62.50	4132.15	.00/14223.85	.00	.34	72.1 °F
APR	220.83	3249.73	.00/13338.27	.00	44.18	70.8 °F
MAY	.00	5042.31	.00/10556.39	.00	.00	75.3 °F
JUN	12.50	3367.30	.00/ 9389.09	.00	.00	74.3 °F
JUL	.00	2106.67	20.83/ 9462.27	.00	59.74	81.8 °F
AUG	70.83	1881.97	20.83/ 9797.46	.00	114.08	81.0 °F
SEP	204.17	1798.39	20.83/10229.31	.00	161.43	84.5 °F
OCT	220.83	1390.48	20.83/11076.99	.00	243.10	75.0 °F
NOV	679.17	1350.04	20.83/12193.64	.00	399.97	69.0 °F
DEC	2162.50	1202.95	20.83/14278.11	.00	1135.50	63.9 °F
SUM	3800.00	29612.55	20.83/14278.11	.00	2383.48	
AVG.	316.67	2467.71		.00	198.62	74.0 °F

1985 WATER BUDGET SUMMARY

	RAINFALL VOLUME (CU.FT.)	E.T. VOLUME (CU.FT.)	SURFACE/SUBSURFACE STORAGE (CU.FT.)	DEEP PERCOLATION (CU.FT.)	SURFACE RUNOFF (CU.FT.)	AVERAGED TEMPERATURE (°F)
JAN	337.50	949.41	20.83/15580.57	.00	346.04	64.5 °F
FEB	683.33	2350.03	20.83/15667.49	.00	288.06	64.9 °F
MAR	245.83	3712.55	.00/14445.60	.00	36.43	63.2 °F
APR	50.00	4048.61	.00/12634.49	.00	.00	70.2 °F
MAY	8.33	4512.31	.00/10390.93	.00	.00	68.9 °F
JUN	.00	3719.90	.00/ 8858.53	.00	.00	73.4 °F

=====
 ==> END OF WATER BUDGET SIMULATION <==

APPENDIX B
COMPUTER CODE

C THIS IS A SURFACE-SUBSURFACE WATER BUDGET PROGRAM
 C

```

    CHARACTER IMON(12)*3,KO*1,IFILE*15,OFFILE*15
    DIMENSION IDAY(12),GI(12)
    DIMENSION TEMP(31),RAIN(31),EVP(12)
    DATA PR/O./,PT/O./,PIG/O./,PG/O./,PP/O./,PB/O./,
  C   PI/O./,PS/O./,PII/O./,PP1/O./
    DATA IMON/'JAN','FEB','MAR','APR','MAY','JUN',
  C   'JUL','AUG','SEP','OCT','NOV','DEC'/
    DATA IDAY/31,28,31,30,31,30,31,31,30,31,30,31/
    DATA GI/.4,.8,1.,1.,1.,.8,.4,.4,.4,.4,.4,.4/
    DATA KO/'Y'/
    DATA IYEAR/1962/,IEND/1987/
    DATA XDI/O./,XDPI/O./,XDPI1/O./,XDPP/O./,XDPP1/O./,VOLSUR/O./,
  C   TTO/O./,TET/O./,TSUB/O./,TSUR/O./,TPER/O./,TRUN/O./

```

C
 C OPEN FILES
 C

```

    OPEN(UNIT=1,FILE='TEMP.FIL',STATUS='OLD')
    OPEN(UNIT=2,FILE='RAIN.FIL',STATUS='OLD')
    OPEN(UNIT=3,FILE='EVAP.FIL',STATUS='OLD')

```

C
 C INPUT SUBAREA INFORMATION
 C

```

35  WRITE(*,*)' SURFACE-SUBSURFACE WATER BUDGET MODEL'
    WRITE(*,*)' ENTER A [1] TO CREAT A NEW DATA FILE'
    WRITE(*,*)' OR A [2] TO EXECUTE AN EXISTING FILE'
    WRITE(*,*)' OR A [3] TO EXIST PROGRAM'
    WRITE(*,4)
    READ(*,*,ERR=35)JKODE
    IF(JKODE.EQ.1)GO TO 37
    IF(JKODE.EQ.2)GO TO 90
    IF(JKODE.EQ.3)STOP ' '
    GO TO 35
37  WRITE(*,*)' ENTER THE FILE NAME THAT STORES THE INPUT DATA'
    WRITE(*,4)
    READ(*,34)IFILE
34  FORMAT(A15)
    OPEN(UNIT=4,FILE=IFILE,STATUS='NEW')
91  WRITE(*,1)
1   FORMAT(' ENTER TOTAL AREA (SQUARE FEET) = ',\ )
    READ(*,*,ERR=91)AREA
92  WRITE(*,2)
2   FORMAT(' ENTER MAXIMUM SUBSURFACE STORAGE (CUBIC FEET) = ',\ )
    READ(*,*,ERR=92)SUBMAX
25  WRITE(*,21)SUBMAX
21  FORMAT(' ENTER INITIAL SUBSURFACE STORAGE (CUBIC FEET)',/,
1   ' ALLOWABLE VALUE IS BETWEEN [0] AND [',F9.2,']')
    WRITE(*,4)
    READ(*,*,ERR=25)VOLSUB
    IF(VOLSUB.LT.0. .OR. VOLSUB.GT.SUBMAX)GO TO 25
20  WRITE(*,3)
3   FORMAT(' ENTER DRIVE WAY AND ROOF COVERAGE (%)',/,
1   ' ALLOWABLE VALUE IS BETWEEN [0] AND [100]')
    WRITE(*,4)

```

```

4  FORMAT('====>',\ )
   READ(*,*,ERR=20)PR
   IF(PR.LT.0. .OR. PR.GT.100.)GO TO 20
   XP=100.-PR
   IF(XP.EQ.0.)GO TO 60
30  WRITE(*,5)XP
   5  FORMAT('  ENTER TREE AND BUSH COVERAGE (%)',/,
1  '  ALLOWABLE VALUE IS BETWEEN [0] AND ['F4.1,']')
   WRITE(*,4)
   READ(*,*,ERR=30)PT
   IF(PT.LT.0. .OR. PT.GT.XP)GO TO 30
93  WRITE(*,*)'  ENTER DEPTH (INCHES) OF INTERCEPTION'
   WRITE(*,4)
   READ(*,*,ERR=93)DINT
   XP=XP-PT
   IF(XP.EQ.0.)GO TO 60
40  WRITE(*,6)XP
   6  FORMAT('  ENTER CONCRETE WALK WAY AND PATIO COVERAGE (%)',/,
1  '  ALLOWABLE VALUE IS BETWEEN [0] AND ['F4.1,']')
   WRITE(*,4)
   READ(*,*,ERR=40)PIG
   IF(PIG.LT.0. .OR. PIG.GT.XP)GO TO 40
   XP=XP-PIG
   IF(XP.EQ.0.)GO TO 60
50  WRITE(*,7)XP
   7  FORMAT('  ENTER GRASS COVERAGE (%)',/,
1  '  ALLOWABLE VALUE IS BETWEEN [0] AND ['F4.1,']')
   WRITE(*,4)
   READ(*,*,ERR=50)PG
   IF(PG.LT.0. .OR. PG.GT.XP)GO TO 50
   XP=XP-PG
   IF(XP.EQ.0.)GO TO 60
55  WRITE(*,*)'  IMPERVIOUS PONDING AREA'
   WRITE(*,31)XP
31  FORMAT('  ENTER PONDING AREA(%) THAT DRAINS TO IMPERVIOUS ',
1  'AREA',/, '  ALLOWABLE VALUE IS BETWEEN [0] AND ['F4.1,']')
   WRITE(*,4)
   READ(*,*,ERR=55)PI1
   IF(PI1.LT.0. .OR. PI1.GT.XP)GO TO 55
   DPI1=0.
   IF(PI1.EQ.0.)GO TO 65
94  WRITE(*,*)'  ENTER PONDING DEPTH (INCHES) '
   WRITE(*,4)
   READ(*,*,ERR=94)DPI1
   XP=XP-PI1
   IF(XP.EQ.0.)GO TO 60
65  WRITE(*,32)XP
32  FORMAT('  ENTER PONDING AREA(%) THAT DRAINS TO PERVIOUS AREA',
1  /, '  ALLOWABLE VALUE IS BETWEEN [0] AND ['F4.1,']')
   WRITE(*,4)
   READ(*,*,ERR=65)PI
   IF(PI.LT.0. .OR. PI.GT.XP)GO TO 65
   DPI=0.
   IF(PI.EQ.0.)GO TO 56
96  WRITE(*,*)'  ENTER PONDING DEPTH (INCHES) '
   WRITE(*,4)
   READ(*,*,ERR=96)DPI
   XP=XP-PI
   IF(XP.EQ.0.)GO TO 60

```

```

56  WRITE(*,*)' PERVIOUS PONDING AREA'
    WRITE(*,31)XP
    WRITE(*,4)
    READ(*,*,ERR=56)PP1
    IF(PP1.LT.0. .OR. PP1.GT.XP)GO TO 56
    DPP1=0.
    IF(PP1.EQ.0.)GO TO 66
97  WRITE(*,*)' ENTER PONDING DEPTH (INCHES)'
    WRITE(*,4)
    READ(*,*,ERR=97)DPP1
    XP=XP-PP1
    IF(XP.EQ.0.)GO TO 60
66  WRITE(*,32)XP
    WRITE(*,4)
    READ(*,*,ERR=66)PP
    IF(PP.LT.0. .OR. PP.GT.XP)GO TO 66
    DPP=0.
    IF(PP.EQ.0.)GO TO 67
98  WRITE(*,*)' ENTER PONDING DEPTH (INCHES)'
    WRITE(*,4)
    READ(*,*,ERR=98)DPP
67  XP=XP-PP
    IF(XP.EQ.0.)GO TO 60
70  WRITE(*,33)XP
33  FORMAT(' ENTER AREA (%) SLOPE AWAY FROM HOUSE',/,
1  ' ALLOWABLE VALUE IS BETWEEN [0] AND [',F4.1,']')
    WRITE(*,4)
    READ(*,*,ERR=70)PS
    IF(PS.LT.0. .OR. PS.GT.XP)GO TO 70
    PB=XP-PS
    IF(PB.NE.0.)WRITE(*,8)PB
8  FORMAT(' PERCENT OF BARE LAND AREA IS ',F4.1,' %',/)
C
C  SAVE THE INPUT FILE
C
60  IF(JKODE.NE.1)GO TO 61
    WRITE(4,*)AREA,SUBMAX,VOLSUB
    WRITE(4,*)PR,PT,DINT,PIG
    WRITE(4,*)PG,PI1,DPI1,PI,DPI,PP1,DPP1,PP,DPP,PS,PB
    WRITE(*,*)' '
    WRITE(*,46)IFILE
46  FORMAT(/,2X,A15,'...DATA FILE HAS BEEN CREATED',/)
    CLOSE (UNIT=4)
    GO TO 35
C
C  READ DATA FORM INPUT FILE
C
90  WRITE(*,*)' ENTER THE FILE NAME THAT STORES THE INPUT DATA'
    WRITE(*,4)
    READ(*,34)IFILE
    WRITE(*,*)' ENTER THE FILE NAME THAT STORES THE OUTPUT RESULTS'
    WRITE(*,4)
    READ(*,34)OFILE
    OPEN(UNIT=4,FILE=IFILE,STATUS='OLD')
    READ(4,*)AREA,SUBMAX,VOLSUB
    READ(4,*)PR,PT,DINT,PIG
    READ(4,*)PG,PI1,DPI1,PI,DPI,PP1,DPP1,PP,DPP,PS,PB
    CLOSE (UNIT=4)
C

```

C ENTER MODEL VARIABLES

```

C
61  WRITE(*,*)' INFILTRATION MODEL IS APPROXIMATED BY'
    WRITE(*,*)'      A CONSTANT SOIL LOSS RATE '
    WRITE(*,15)
15  FORMAT(/,' ENTER CONSTANT SOIL LOSS RATE (IN/HR) = ',\ )
    READ(*,*,ERR=60)FO
    DINF=FO*24.
62  WRITE(*,*)' ENTER PERCENT (%) OF GROUNDWATER STORAGE THAT'
    WRITE(*,*)' CAN BE USED BY E.T. AFTER SUBSURFACE STORAGE WAS'
    WRITE(*,*)' DEPLETED BY E.T.'
    WRITE(*,4)
    READ(*,*,ERR=62)PGR
    IF(PGR.LT.0. .OR. PGR.GT.100.)GO TO 62
991 WRITE(*,*)' ENTER LONG TERM AVERAGE IRRIGATION WATER DEPTH (IN)'
    WRITE(*,4)
    READ(*,*,ERR=991)DIRR
    WRITE(*,27)
27  FORMAT(' DO YOU WANT TO OUTPUT A DAILY WATER BUDGET FOR',/,
1  ' A USER SPECIFIED MONTH AND YEAR (Y/N) =====> ',\ )
    READ(*,23)KY
23  FORMAT(A1)
    IF(KY.NE.KO)GO TO 80
75  WRITE(*,24)
24  FORMAT(' ENTER SPECIFIED MONTH BETWEEN [1] AND [12]')
    WRITE(*,4)
    READ(*,*,ERR=75)ISM
    IF(ISM.LT.1 .OR. LSM.GT.12)GO TO 75
85  WRITE(*,26)IYEAR,IEND
26  FORMAT(' ENTER SPECIFIED YEAR BETWEEN [' ,I4,'] AND [' ,I4,']')
    WRITE(*,4)
    READ(*,*,ERR=85)ISY
    IF(ISY.LT.IYEAR .OR. ISY.GT.IEND)GO TO 85
C..COMPOSED RATIO OF GROWTH INDEX TO PAN EVAPORATION
80  XK=0.
    DA=PT+PG+PS+PI+PP
    DB=PT*1.5+(PS+PI+PP)*1.2+PG
    IF(DA.NE.0.)XK=DB/DA
    
```

C OUTPUT SUBAREA INFORMATION

```

C
    OPEN(UNIT=7,FILE=OFILE,STATUS='UNKNOWN')
    WRITE(7,9)PR,PT,PIG
9  FORMAT(3(/),
1  5X,' RAINFALL',//,
2  2X,35(' | '),//,3X,34(' | '),//,
3  13X,'^',/,13X,'|',/,13X,'|',/,6X,' EVAPORATION',/,13X,'|',/,
3  5X,' -----',/,
3  5X,' | DRIVE-WAY AND |',/,
4  5X,' | ROOF COVER |',/,
5  5X,' |',3X,F4.1,' % | -----',14X,'^',/,
6  6X,17(' -'),' | TREE COVER |',14X,'|',/,
7  13X,'| |',3X,F4.1,' % |',9X,'EVAPORATION',/,
8  6X,' | -----',14X,'|',/,
9  6X,' |',11X,21(' -'),/,
1 6X,' |',21X,' | CONCRETE WALK WAY |',/,
2 6X,' |',21X,' | AND PATIO COVER |',/,
3 6X,' |',9X,'|',11X,'| ^ |',7X,F4.1,' % |',/,
4 6X,' |',9X,'|',11X,'| | -----',/,
    
```



```

47  FORMAT(3X,'11. It is assumed that the depth of interception for',
1   ' tree and bush',/,8X,'is ',F3.1,' inches.',//,3X,'12. Ponding',
2   ' depth of impervious area that drains to impervious area',/,8X,
3   'is ',F3.1,' inches.',//,3X,'13. Ponding',
2   ' depth of impervious area that drains to pervious area',/,8X,
3   'is ',F3.1,' inches.',//,3X,'14. Ponding',
2   ' depth of pervious area that drains to impervious area',/,8X,
3   'is ',F3.1,' inches.',//,3X,'15. Ponding',
2   ' depth of pervious area that drains to pervious area',/,8X,
3   'is ',F3.1,' inches.',6(/))

```

```

C
C
C

```

```

YEARLY WATER BUDGET SIMULATION LOOP

```

```

DO 1000 II=IYEAR,IEND
WRITE(7,11)II
11  FORMAT(///,5X,I4,' WATER BUDGET SUMMARY',//,8X,'RAINFALL',3X,
1   'E.T. SURFACE/SUBSURFACE',5X,'DEEP',5X,'SURFACE',3X,'AVERAGED',
1   '/',9X,'VOLUME',3X,'VOLUME',7X,'STORAGE',7X,'PERCOLATION',2X,
2   'RUNOFF',2X,'TEMPERATURE',/,8X,'(CU.FT.) (CU.FT.) (CU.FT.)',
3   8X,'(CU.FT.)',2X,'(CU.FT.)',5X,'(°F)',/,7X,71('-')//)
YPER=0.
YTO=0.
YET=0.
YRUN=0.
YTEMP=0.
READ(3,*,END=9999)(EVP(I),I=1,12)

```

```

C
C
C

```

```

MONTHLY WATER BUDGET SIMULATION LOOP

```

```

DO 1100 JJ=1,12
IF(II.EQ.IYEAR .AND. JJ.LT.9)GO TO 1200
VOLTO=0.
VOLET=0.
VOLRUN=0.
VOLPER=0.
TTEMP=0.
IDAY(2)=28
IF(JJ.EQ.2 .AND. MOD(II,4).EQ.0)IDAY(2)=29

```

```

C
C
C

```

```

INPUT MONTHLY TEMPERATURE AND RAINFALL DATA

```

```

READ(1,*,END=9999)(TEMP(I),I=1,IDAY(JJ))
READ(2,*,END=9999)(RAIN(I),I=1,IDAY(JJ))

```

```

C
C
C

```

```

DAILY WATER BUDGET SIMULATION LOOP

```

```

DO 110 I=1,IDAY(JJ)
110  TTEMP=TTEMP+TEMP(I)
    XXK=XK*GI(JJ)
    DO 100 I=1,IDAY(JJ)
    ET=EVP(JJ)
    DEPTH=RAIN(I)
    VOLTO=VOLTO+DEPTH*AREA/12.
C..ESTIMATION OF ET AND PET
    TFRA=TEMP(I)/TTEMP
    ET=ET*TFRA
    VOLABC=VOLSUB+(PP+PS+PP1)*DEPTH*AREA*.01/12.
    PET=XXK*ET*VOLABC/SUBMAX/.115

```

C..ROOF COVER

IF(PR.EQ.O.)GO TO 210
A=AREA*PR*.01/12.
IF(DEPTH.LT.ET)GO TO 200
VOLRUN=VOLRUN+(DEPTH-ET)*A
VOLET=VOLET+ET*A
GO TO 210

200 VOLET=VOLET+DEPTH*A

210 CONTINUE

C..CONCRETE WALK WAY AND PATIO COVER

IF(PIG.EQ.O.)GO TO 250
A=AREA*PIG*.01/12.
DIG=0.
IF(DEPTH.LE.ET)GO TO 220
VOLET=VOLET+ET*A
DIG=DEPTH-ET
GO TO 230

220 VOLET=VOLET+DEPTH*A

C..TREE AND BUSH COVERAGE

230 IF(PT.EQ.O.)GO TO 240
DIT=0.
A=AREA*PT*.01/12.
XDI=XDI+DEPTH
IF(XDI.GT.ET)GO TO 235
VOLET=VOLET+XDI*A
XDI=0.
GO TO 240

235 VOLET=VOLET+ET*A

XDI=XDI-ET

IF(XDI.LT.DINT)GO TO 240

DIT=XDI-DINT

XDI=DINT

C..IMPERVIOUS PONDING AREA

C....OVERLAND FLOW TO IMPERVIOUS AREA

240 IF(PI1.EQ.O.)GO TO 245
A=AREA*PI1*.01/12.
XDPI1=XDPI1+DEPTH+DIRR
XET=AMAX1(ET,PET)
IF(XDPI1.GT.XET)GO TO 243
VOLET=VOLET+XDPI1*A
XDPI1=0.
GO TO 245

243 VOLET=VOLET+XET*A

XDPI1=XDPI1-XET

IF(XDPI1.LT.DPI1)GO TO 245

VOLRUN=VOLRUN+(XDPI1-DPI1)*A

XDPI1=DPI1

C....OVERLAND FLOW TO PERVIOUS AREA

245 IF(PI.EQ.O.)GO TO 255
A=AREA*PI*.01/12.
XDPI=XDPI+DEPTH+DIRR
XET=AMAX1(ET,PET)
DPIP=0.
IF(XDPI.GT.XET)GO TO 253
VOLET=VOLET+XDPI*A
XDPI=0.
GO TO 255

253 VOLET=VOLET+XET*A

XDPI=XDPI-XET

IF(XDPI.LT.DPI)GO TO 255

```

DPIP=XDPI-DPI
XDPI=DPI
C..Pervious Ponding Area
C....OVERLAND FLOW TO IMPERVIOUS AREA
255 IF(PP1.EQ.0.)GO TO 257
A=AREA*PP1*.01/12.
XDPP1=XDPP1+DEPTH+DIRR
XET=AMAX1(ET,PET)
CALL BUDGET(XDPP1,XET,A,SUBMAX,VOLSUB,VOLPER,DINF,DPP1,
C          DG1,VOLET,VOLRUN,PGR)
VOLRUN=VOLRUN+DG1*A
C....OVERLAND FLOW TO Pervious AREA
257 IF(PP.EQ.0.)GO TO 250
A=AREA*PP*.01/12.
XDPP=XDPP+DEPTH+DIRR
XET=AMAX1(ET,PET)
CALL BUDGET(XDPP,XET,A,SUBMAX,VOLSUB,VOLPER,DINF,DPP,
C          DG,VOLET,VOLRUN,PGR)
C...GRASS COVER
250 IF(PG.EQ.0.)GO TO 260
DAVE=((DEPTH+DIRR)*PG+DIT*PT+DG*PP+DIG*PIG+DPIP*PI)/PG
A=AREA*PG*.01/12.
CALL BUDGET(DAVE,PET,A,SUBMAX,VOLSUB,VOLPER,DINF,0.,
C          DUM,VOLET,VOLRUN,PGR)
C..BARE LAND
260 IF(PB.EQ.0.)GO TO 270
A=AREA*PB*.01/12.
CALL BUDGET(DEPTH,ET,A,SUBMAX,VOLSUB,VOLPER,DINF,0.,
C          DUM,VOLET,VOLRUN,PGR)
C..AREA SLOPE AWAY FROM HOUSE
270 A=AREA*PS*.01/12.
CALL BUDGET(DEPTH,PET,A,SUBMAX,VOLSUB,VOLPER,DINF,0.,
C          DUM,VOLET,VOLRUN,PGR)
C..CALCULATE SURFACE PONDING VOLUME
VOLSUR=(XDI*PT+XDPI*PI+XDPI1*PI1+XDPP*PP+XDPP1*PP1)*AREA*.01/12.
C..END OF DAILY WATER BUDGET
C..SUMMARY OF DAILY WATER BUDGET
IF(JJ.NE.ISM .OR. II.NE.ISY)GO TO 100
IF(I.EQ.1)GO TO 400
DTP=VOLTO-TTO
DET=VOLET-TET
DSUB=VOLSUB-TSUB
DRUN=VOLRUN-TRUN
DPER=VOLPER-TPER
DSUB=VOLSUB-TSUB+DPER
DSUR=VOLSUR-TSUR
C..OUTPUT WATER BUDGET
400 WRITE(7,211)I,VOLTO,VOLET,VOLSUB,VOLPER,VOLSUR,VOLRUN
211 FORMAT(/,5X,'MODEL TIME = ',I2,' DAYS',/,
1 5X,'TOTAL RAINFALL VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'TOTAL EVAPOTRANSPIRATION VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'TOTAL SUBSURFACE STORAGE VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'TOTAL DEEP PERCOLATION VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'TOTAL SURFACE STORAGE VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'TOTAL SURFACE RUNOFF VOLUME = ',F12.2,' CUBIC FEET')
IF(I.NE.1)WRITE(7,212)DTP,DET,DSUB,DPER,DSUR,DRUN
212 FORMAT(/,
1 5X,'DAILY RAINFALL VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'DAILY EVAPOTRANSPIRATION VOLUME = ',F12.2,' CUBIC FEET',/,

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1 5X,'DAILY SUBSURFACE STORAGE VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'DAILY DEEP PERCOLATION VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'DAILY SURFACE STORAGE VOLUME = ',F12.2,' CUBIC FEET',/,
1 5X,'DAILY SURFACE RUNOFF VOLUME = ',F12.2,' CUBIC FEET',/)
IF(VOLSUB.EQ.SUBMAX)WRITE(7,213)
213 FORMAT(5X,'*** SUBSURFACE STORAGE IS FULL ***')
IF(I.NE.1 .AND. DRUN.EQ.0.)WRITE(7,215)
215 FORMAT(5X,'*** SURFACE RUNOFF IS ZERO ***')
IF(DSUB.LT.0.)WRITE(7,216)
216 FORMAT(5X,'*** SUBSURFACE STORAGE IS USED BY ACTUAL',
1 ' EVAPOTRANSPIRATION ***')
IF(VOLSUB.EQ.0.)WRITE(7,217)
217 FORMAT(5X,'*** SUBSURFACE STORAGE IS EMPTY ***')
WRITE(7,218)
218 FORMAT(4X,70('='))
TTO=VOLTO
TET=VOLET
TSUB=VOLSUB
TSUR=VOLSUR
TPER=VOLPER
TRUN=VOLRUN
100 CONTINUE
C..OUTPUT MONTHLY WATER BUDGET
TTEMP=TTEMP/REAL(IDAY(JJ))
WRITE(7,12)IMON(JJ),VOLTO,VOLET,VOLSUR,VOLSUB,VOLPER,VOLRUN,TTEMP
12 FORMAT(2X,A3,3X,F8.2,1X,F8.2,1X,F8.2,'/',F8.2,4X,F8.2,2X,F8.2,
1 3X,F5.1,' °F')
GO TO 1300
1200 WRITE(7,42)IMON(JJ)
42 FORMAT(2X,A3,3X,'NO RAINFALL DATA')
C..YEARLY TOTAL SUMMATION
1300 YTO=YTO+VOLTO
YET=YET+VOLET
YRUN=YRUN+VOLRUN
YTEMP=YTEMP+TTEMP
YPER=YPER+VOLPER
1100 CONTINUE
C..OUTPUT YEARLY TOTAL AND AVERAGED VALUES
WRITE(7,13)YTO,YET,VOLSUR,VOLSUB,YPER,YRUN
13 FORMAT(/,78('-'),/,2X,'SUM',3X,F8.2,1X,F8.2,1X,F8.2,'/',F8.2,4X,
1 F8.2,2X,F8.2)
C..YEARLY AVERAGING
YTO=YTO/12.
YET=YET/12.
YRUN=YRUN/12.
YTEMP=YTEMP/12.
YPER=YPER/12.
IF(II.EQ.IYEAR)WRITE(7,14)
14 FORMAT(2X,'AVG.',/,78('*'),///)
IF(II.NE.IYEAR)WRITE(7,44)YTO,YET,YPER,YRUN,YTEMP
44 FORMAT(2X,'AVG.',2X,F8.2,1X,F8.2,22X,F8.2,2X,F8.2,3X,F5.1,' °F',/,
1 78('*'),///)
1000 CONTINUE
C
C END OF SIMULATION
C
9999 WRITE(7,22)
22 FORMAT(/,78('='),/, ' ==> END OF WATER BUDGET SIMULATION <==',/)
WRITE(*,22)
C
CLOSE (UNIT=7)

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WRITE(*,41)OFIL
41  FORMAT(' NOTE: YOUR OUTPUT IS STORED IN [ ',A15,']',///)
C
GO TO 35
C
END
C
SURFACE-SUBSURFACE WATER BUDGET PROGRAM
C
SUBROUTINE BUDGET(DEPTH,AET,A,SUBMAX,VOLSUB,VOLPER,
C              DINF,DP,DG,VOLET,VOLRUN,PGR)
C..INITIALIZATION OF VARIABLE
DG=0.
C
C WATER BUDGET
C
AVIVOL=VOLSUB
IF(AVIVOL.NE.0.)GO TO 150
PG=PGR/100.
AVIVOL=PG*VOLPER
VOLPER=VOLPER*(1.-PG)
150  ETVOL=AET*A
RAVOL=DEPTH*A
IF(DEPTH.GE.AET)GO TO 100
IF(RAVOL+AVIVOL.GT.ETVOL)GO TO 200
C..DEPLETION ALL OF THE AVAILABLE SUBSURFACE STORAGE BY AET
VOLET=VOLET+RAVOL+AVIVOL
VOLSUB=0.
IF(DP.NE.0.)DEPTH=0.
RETURN
C..DEPLETION PART OF THE AVAILABLE SUBSURFACE STORAGE BY AET
200  VOLSUB=VOLSUB+RAVOL-ETVOL
VOLET=VOLET+ETVOL
IF(DP.NE.0.)DEPTH=0.
RETURN
C..INFILTRATION TO SUBSURFACE STORAGE
100  IF(DINF.GE.DEPTH-AET)GO TO 110
C..PONDING OR EXCESS SURFACE RUNOFF FROM INFILTRATION
IF(DP.EQ.0.)GO TO 105
XD=DEPTH-AET-DINF
DEPTH=XD
IF(XD.LT.DP)GO TO 105
DG=XD-DP
DEPTH=DP
105  VOLSUB=VOLSUB+DINF*A
VOLET=VOLET+ETVOL
IF(DP.EQ.0.)VOLRUN=VOLRUN+(DEPTH-AET-DINF)*A
GO TO 120
C..TOTAL INFILTRATION
110  VOLSUB=VOLSUB+(DEPTH-AET)*A
VOLET=VOLET+ETVOL
IF(DP.NE.0.)DEPTH=0.
C..CHECK DEEP PERCOLATION
120  IF(VOLSUB.LT.SUBMAX)RETURN
VOLPER=VOLPER+VOLSUB-SUBMAX
VOLSUB=SUBMAX
RETURN
END

```

Note: TEMP.FIL, RAIN.FIL, and EVAP.FIL files store temperature, rainfall, and evaporation data, respectively.